# Experimental Probability

Q

#### **ESSENTIAL QUESTION**

How can you use experimental probability to solve real-world problems?







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7.NS.3, 7.SP.6

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# Are Ready

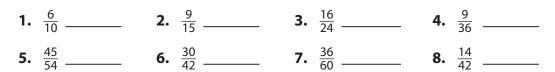
Complete these exercises to review skills you will need for this module.

#### **Simplify Fractions**

#### **EXAMPLE** Simplify <u>12</u>

21	
	List all the factors of the numerator and denominator.
21: 1,3 7, 21	Circle the greatest common factor (GCF).
$\frac{12 \div 3}{21 \div 3} = \frac{4}{7}$	Divide the numerator and denominator by the GCF.

Write each fraction in simplest form.



#### Write Fractions as Decimals

EXAMPLE	$\frac{13}{25} \rightarrow$	0.52
	23	25)13.00
		- 12.5
		50
		- 50
		0

Write the fraction as a division problem. Write a decimal point and a zero in the dividend. Place a decimal point in the quotient. Write more zeros in the dividend if

Write each fraction as a decimal.

**9.**  $\frac{3}{4}$  \_\_\_\_\_ **10.**  $\frac{7}{8}$  \_\_\_\_\_ **11.**  $\frac{3}{20}$  \_\_\_\_\_ **12.**  $\frac{19}{50}$  \_\_\_\_\_

necessary.

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#### **Percents and Decimals**

EXAMPLE 109% = 100% + 9%Write the percent as the sum of 1 whole  $=\frac{100}{100}+\frac{9}{100}$ and a percent remainder. Write the percents as fractions. = 1 + 0.09Write the fractions as decimals. = 1.09Simplify.

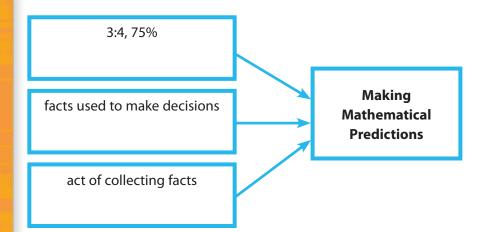
Write each percent as a decimal.

13.	67%	14.	31%	15.	7%	16.	146%
Write	each decimal as	a pe	rcent.				
17.	0.13	18.	0.55	19.	0.08	20.	1.16

Reading Start-Up

#### **Visualize Vocabulary**

Use the 🖌 words to complete the graphic. You can put more than one word in each box.



#### **Understand Vocabulary**

Match the term on the left to the definition on the right.

1.	probability	Α.	Measures the likelihood that the event will occur.
2.	trial	В.	A set of one or more outcomes.
3.	event	с.	Each observation of an experiment.

#### Vocabulary

#### **Review Words**

- ✓ data (datos)
- ✓ observation (observación)
- ✓ percent (*porcentaje*)
- ✓ ratio (razón)

#### **Preview Words**

complement (complemento) compound event (suceso compuesto) event (suceso) experiment (experimento) experimental probability (probabilidad experimental) outcome (resultado) probability (probabilidad) simple event (suceso simple) simulation (simulación) trial (prueba)

#### **Active Reading**

**Pyramid** Before beginning the module, create a rectangular pyramid to help you organize what you learn. Label each side with one of the lesson titles from this module. As you study each lesson, write important ideas, such as vocabulary, properties, and formulas, on the appropriate side.



#### MODULE 12 Unpacking the Standards

Understanding the standards and the vocabulary terms in the standards will help you know exactly what you are expected to learn in this module.

#### COMMON CORE 7.SP.6

Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.

#### **Key Vocabulary**

simple event (suceso simple)

An event consisting of only one outcome.

#### experimental probability (probabilidad experimental)

The ratio of the number of times an event occurs to the total number of trials, or times that the activity is performed.

#### What It Means to You

You will use experimental probabilities to make predictions and solve problems.

#### **UNPACKING EXAMPLE 7.SP.6**

Caitlyn finds that the experimental probability of her making a goal in hockey is 30%. Out of 500 attempts to make a goal, about how many could she predict she would make?

 $\frac{3}{10} \cdot 500 = x$ 

150 = *x* 

Caitlyn can predict that she will make about 150 of the 500 goals that she attempts.



#### COMMON CORE 7.SP.7b

Develop a probability model (which may not be uniform) by observing frequencies in data generated from a chance process.

#### **Key Vocabulary**

#### sample space (espacio muestral)

All possible outcomes of an experiment.



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#### What It Means to You

You will use data to determine experimental probabilities.

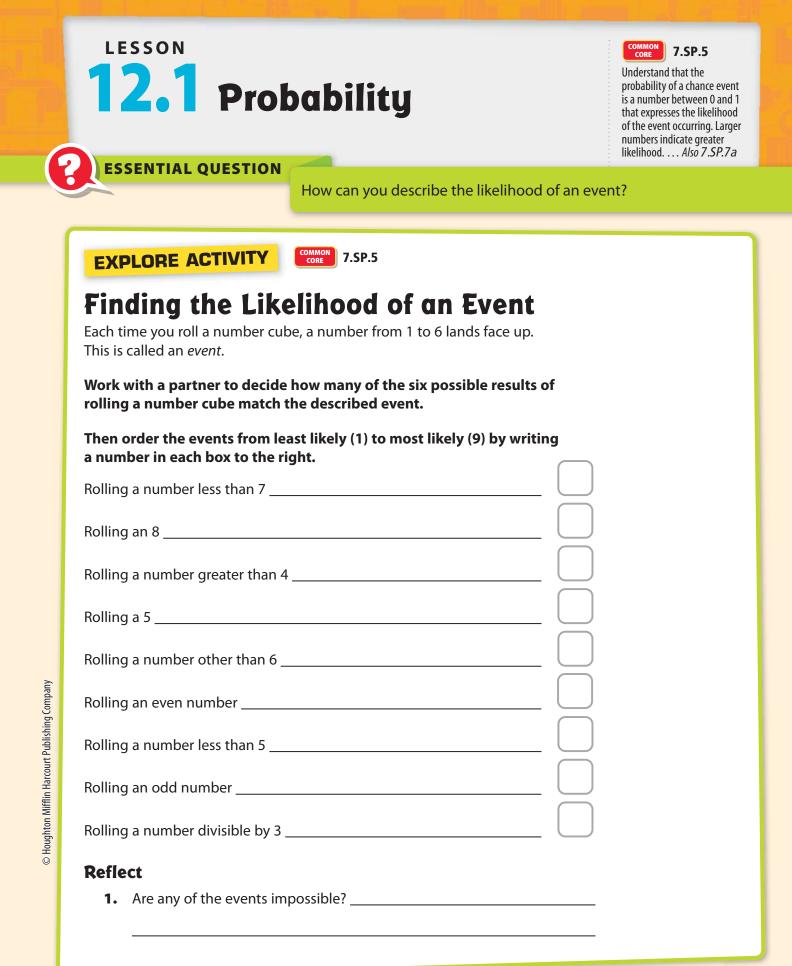
#### **UNPACKING EXAMPLE 7.SP.7b**

Anders buys a novelty coin that is weighted more heavily on one side. He flips the coin 60 times and a head comes up 36 times. Based on his results, what is the experimental probability of flipping a head?

experimental probability =  $\frac{\text{number of times event occurs}}{\text{total number of trials}}$ 

$$=\frac{36}{60}=\frac{3}{5}$$

The experimental probability of flipping a head is  $\frac{3}{5}$ .





## **Describing Events**

An **experiment** is an activity involving chance in which results are observed. Each observation of an experiment is a **trial**, and each result is an **outcome**. A set of one or more outcomes is an **event**.

The **probability** of an event, written *P*(event), measures the likelihood that the event will occur. Probability is a measure between 0 and 1 as shown on the number line, and can be written as a fraction, a decimal, or a percent.

If the event is not likely to occur, the probability of the event is close to 0. If an event is likely to occur, the event's probability is closer to 1.

Impossible	Unlikely	As likely as not	Likely	Certain
 0		<u>1</u> 2		 1
0 0%		0.5 50%		1.0 100%
0%		50%		100%

#### EXAMPLE 1

COMMON CORE 7.SP.5

Tell whether each event is impossible, unlikely, as likely as not, likely, or certain. Then, tell whether the probability is 0, close to 0,  $\frac{1}{2}$ , close to 1, or 1.

A You roll a six-sided number cube and the number is 1 or greater.

This event is certain to happen. Its probability is 1. Because you can roll the numbers 1, 2, 3, 4, 5, and 6 on a number cube, there are 6 possible outcomes.

**B** You roll two number cubes and the sum of the numbers is 3.

This event is unlikely to happen. Its probability is close to 0.

C A bowl contains disks marked with the numbers 1 through 10. You close your eyes and select a disk at random. You pick an odd number.

This event is as likely as not. The probability is  $\frac{1}{2}$ .

Math Talk Mathematical Practices

certain an impossible

event? Explain.

A spinner has 8 equal sections marked
 0 through 7. You spin and land on a prime number.

This event is as likely as not. The probability is  $\frac{1}{2}$ .

Remember that a prime number is a whole number greater than 1 and has exactly 2 divisors, 1 and itself.

#### Reflect

**2.** The probability of event *A* is  $\frac{1}{3}$ . The probability of event *B* is  $\frac{1}{4}$ . What can you conclude about the two events?

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**3.** A hat contains pieces of paper marked with the numbers 1 through 16. Tell whether picking an even number is impossible, unlikely, as likely as not, likely, or certain. Tell whether the probability is 0, close to 0,  $\frac{1}{2}$ , close to 1, or 1.



A sample space is the set of all possible outcomes for an experiment. A sample space can be small, such as the 2 outcomes when a coin is flipped. Or a sample space can be large, such as the possible number of Texas Classic automobile license plates. Identifying the sample space can help you calculate the probability of an event.



7.SP.7a

**Probability of An Event** 

 $P(\text{event}) = \frac{\text{number of outcomes in the event}}{\text{number of outcomes in the sample space}}$ 

#### **EXAMPLE 2**



STEP 1 Find the sample space for a standard number cube.  $\{1, 2, 3, 4, 5, 6\}$ There are 6 possible outcomes. **STEP 2** Find the number of ways to roll an even number. 2, 4, 6 The event can occur 3 ways. Find the probability of rolling an even number. **STEP 3**  $P(\text{even}) = \frac{\text{number of ways to roll an even number}}{\text{number of faces on a number cube}}$  $=\frac{3}{6}=\frac{1}{2}$ Substitute values and simplify. The probability of rolling an even number is  $\frac{1}{2}$ . ò





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#### Find each probability. Write your answer in simplest form.

- **4.** Picking a purple marble from a jar with 10 green and 10 purple
- 5. Rolling a number greater than 4 on a standard number cube.



### **Using the Complement of an Event**

The **complement** of an event is the set of all outcomes in the sample space that are not included in the event. For example, in the event of rolling a 3 on a number cube, the complement is rolling any number other than 3, which means the complement is rolling a 1, 2, 4, 5, or 6.

#### An Event and Its Complement

The sum of the probabilities of an event and its complement equals 1. P(event) + P(complement) = 1

You can apply probabilities to situations involving random selection, such as drawing a card out of a shuffled deck or pulling a marble out of a closed bag.

#### Real **EXAMPLE 3** Norle

There are 2 red jacks in a standard deck of 52 cards. What is the probability of not getting a red jack if you select one card at random?

P(event) + P(complement) = 1

P(red jack) + P(not a red jack) = 1 The probability of getting a red jack is  $\frac{2}{52}$ .

 $\frac{2}{52} + P(\text{not a red jack}) = 1$  Substitute  $\frac{2}{52}$  for P(red jack).

 $\frac{2}{52} + P(\text{not a red jack}) = \frac{52}{52}$  Subtract  $\frac{2}{52}$  from both sides.

 $\frac{-\frac{2}{52}}{P(\text{not a red jack})} = \frac{-\frac{2}{52}}{\frac{50}{52}}$ 

 $P(\text{not a red jack}) = \frac{25}{26}$  Simplify.

The probability that you will not draw a red jack is  $\frac{25}{26}$ . It is likely that you will not select a red jack.

7.SP.7a

marbles.

#### Reflect

**6.** Why do the probability of an event and the probability of its complement add up to 1?



**7.** A jar contains 8 marbles marked with the numbers 1 through 8. You pick a marble at random. What is the probability of not picking the

marble marked with the number 5? \_\_\_\_\_

8. You roll a standard number cube. Use the probability of rolling an even

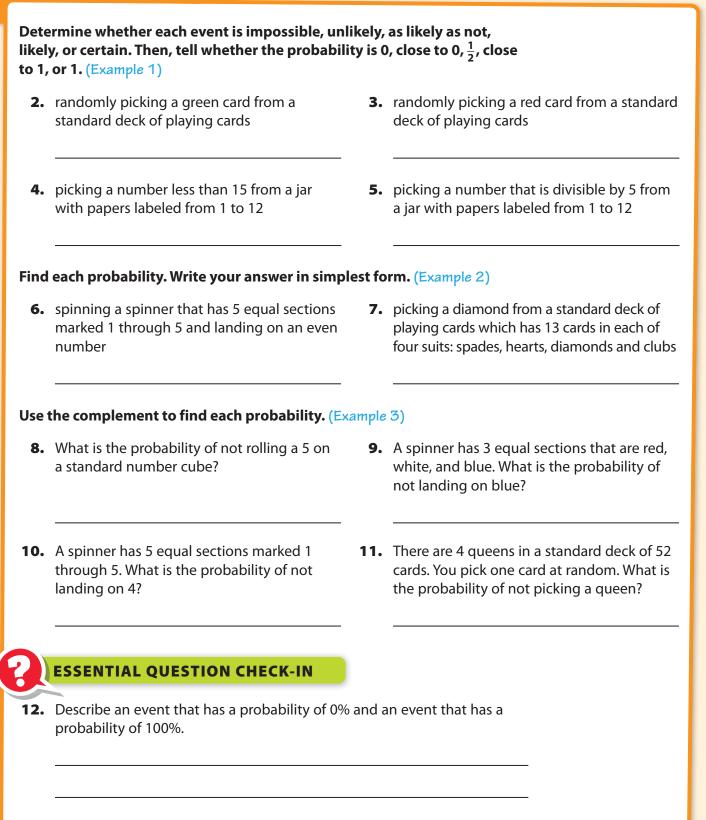
number to find the probability of rolling an odd number.

#### **Guided Practice**

 In a hat, you have index cards with the numbers 1 through 10 written on them. Order the events from least likely to happen (1) to most likely to happen (8) when you pick one card at random. In the boxes, write a number from 1 to 8 to order the eight different events. (Explore Activity)

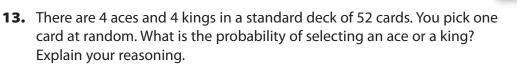
You pick a number greater than 0.
You pick an even number.
You pick a number that is at least 2.
You pick a number that is at most 0.
You pick a number divisible by 3.
You pick a number divisible by 5.
You pick a prime number.
You pick a number less than the greatest prime number.

#### **Guided Practice**



#### Class.





- **14.** There are 12 pieces of fruit in a bowl. Seven of the pieces are apples and two are peaches. What is the probability that a randomly selected piece of fruit will not be an apple or a peach? Justify your answer.
- **15.** Critique Reasoning For breakfast, Clarissa can choose from oatmeal, cereal, French toast, or scrambled eggs. She thinks that if she selects a breakfast at random, it is likely that it will be oatmeal. Is she correct? Explain your reasoning.

16. Draw Conclusions A researcher's garden contains 90 sweet pea plants, which have either white or purple flowers. About 70 of the plants have purple flowers, and about 20 have white flowers. Would you expect that one plant randomly selected from the garden will have purple or white flowers? Explain.



**17.** The power goes out as Sandra is trying to get dressed. If she has 4 white T-shirts and 10 colored T-shirts in her drawer, is it likely that she will pick a colored T-shirt in the dark? What is the probability she will pick a colored T-shirt? Explain your answers.



- **18.** James counts the hair colors of the 22 people in his class, including himself. He finds that there are 4 people with blonde hair, 8 people with brown hair, and 10 people with black hair. What is the probability that a randomly chosen student in the class does not have red hair? Explain.
- **19.** Persevere in Problem Solving A bag contains 8 blue coins and 6 red coins. A coin is removed at random and replaced by three of the other color.
  - a. What is the probability that the removed coin is blue?
  - **b.** If the coin removed is blue, what is the probability of drawing a red coin after three red coins are put in the bag to replace the blue one?
  - **c.** If the coin removed is red, what is the probability of drawing a red coin after three blue coins are put in the bag to replace the red one?



FOCUS ON HIGHER ORDER THINKING

**20.** Draw Conclusions Give an example of an event in which all of the outcomes are not equally likely. Explain.

**21.** Critique Reasoning A box contains 150 black pens and 50 red pens. Jose said the sum of the probability that a randomly selected pen will not be black and the probability that the pen will not be red is 1. Explain whether you agree.

**22.** Communicate Mathematical Ideas A spinner has 7 identical sections. Two sections are blue, 1 is red, and 4 of the sections are green. Suppose the probability of an event happening is  $\frac{2}{7}$ . What does each number in the ratio represent? What outcome matches this probability?

#### Work Area

# **12.2 Experimental Probability of Simple Events**



Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency ... *Also 7.SP.7b* 

**ESSENTIAL QUESTION** 

How do you find the experimental probability of a simple event?

EXPLORE ACTIVITY

COMMON 7.SP.6, 7.SP.7b

# **Finding Experimental Probability**

You can toss a paper cup to demonstrate experimental probability.

- A Consider tossing a paper cup. Fill in the Outcome column of the table with the three different ways the cup could land.
- **B** Toss a paper cup twenty times. Record your observations in the table.

Outcome	Number of Times

#### Reflect

- 1. Do the outcomes appear to be equally likely?
- 2. Describe the three outcomes using the words *likely* and *unlikely*.
- **3.** Use the number of times each event occurred to approximate the probability of each event.
- **4.** Make a Prediction What do you think would happen if you performed more trials?

5. What is the sum of the probabilities in 3?

Outcome	Experimental Probability
Open-end up	$\frac{\text{open-end up}}{20} = \frac{20}{20}$
Open-end down	$\frac{\text{open-end down}}{20} = \frac{20}{20}$
On its side	$\frac{\text{on its side}}{20} = \frac{20}{20}$

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# **Calculating Experimental Probability**

You can use *experimental probability* to approximate the probability of an event. An **experimental probability** of an event is found by comparing the number of times the event occurs to the total number of trials. When there is only one outcome for an event, it is called a **simple event**.

#### **Experimental Probability**

For a given experiment: Experimental probability =  $\frac{\text{number of times the event occurs}}{\text{total number of trials}}$ 



#### EXAMPLE 1 Real

Martin has a bag of marbles. He removed one marble at random, recorded the color and then placed it back in the bag. He repeated this process several times and recorded his results in the table. Find the experimental probability of drawing each color.

Color	Frequency
Red	12
Blue	10
Green	15
Yellow	13

COMMON CORE

7.SP.7b



1) Identify the number of trials: 12 + 10 + 15 + 13 = 50



Complete the table of experimental probabilities. Write each answer as a fraction in simplest form.

Color	Experimental Probability	Substitute the results recorded in the table.
Red	$\frac{\text{frequency of the event}}{\text{total number of trials}} = \frac{12}{50} = \frac{6}{25}$	You can also write each probability as a decimal
Blue	$\frac{\text{frequency of the event}}{\text{total number of trials}} = \frac{10}{50} = \frac{1}{5}$	or as a percent.
Green	$\frac{\text{frequency of the event}}{\text{total number of trials}} = \frac{15}{50} = \frac{3}{10}$	
Yellow	$\frac{\text{frequency of the event}}{\text{total number of trials}} = \frac{13}{50}$	

#### Reflect

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**6.** Communicate Mathematical Ideas What are two different ways you could find the experimental probability of the event that Martin does **not** draw a red marble?



7. A spinner has three unequal sections: red, yellow, and blue. The table shows the results of Nolan's spins. Find the experimental probability of landing on each color. Write your answers in simplest form.

Color	Frequency
Red	10
Yellow	14
Blue	б

7.SP.6

Since the team has

34 chances at bat.

34 times.

you must draw a card



Will everyone who does this experiment get the same results?

Math On the

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My Notes

# Making Predictions with Experimental Probability

A **simulation** is a model of an experiment that would be difficult or inconvenient to actually perform. You can use a simulation to find an experimental probability and make a prediction.

EXAMPLE 2

A baseball team has a batting average of 0.250 so far this season. This means that the team's players get hits in 25% of their chances at bat. Use a simulation to predict the number of hits the team's players will have in their next 34 chances at bat.

**STEP 1** Choose a model.

Batting average =  $0.250 = \frac{250}{1,000} = \frac{1}{4}$ 

A standard deck of cards has four suits, hearts, diamonds, spades, and clubs. Since  $\frac{1}{4}$  of the cards are hearts, you can let hearts represent a "hit." Diamonds, clubs, and spades then represent "no hit."

**STEP 2** Perform the simulation.

Draw a card at random from the deck, record the result, and put the card back into the deck. Continue until you have drawn and replaced 34 cards in all.

(H = heart, D = diamond, C = club, S = spade)

Н	D	D	S	Н	С	Н	S	D	Н	С	D	С	С	D	Н	Н
S	D	D	Н	С	С	Н	С	Н	Н	D	S	9	S	С	Н	D

**STEP 3** Make a prediction.

Count the number of hearts in the simulation.

Since there are 11 hearts, you can predict that the team will have 11 hits in its next 34 chances at bat.





 A toy machine has equal numbers of red, white, and blue foam balls which it releases at random. Ross wonders which color ball will be released next. Describe how you could use a standard number cube to predict the answer.

#### **Guided Practice**

 A spinner has four sections lettered A, B, C, and D. The table shows the results of several spins. Find the experimental probability of spinning each letter as a fraction in simplest form, a decimal, and a percent. (Explore Activity and Example 1)

Letter	А	В	С	D
Frequency	14	7	11	8

C:\_\_\_\_\_

A:\_\_\_\_\_

B:		
D:		

2. Rachel's free-throw average for basketball is 60%. She wants to predict how many times in the next 50 tries she will make a free throw. Describe how she could use 10 index cards to predict the answer. (Example 2)

#### **ESSENTIAL QUESTION CHECK-IN**

**3.** Essential Question Follow Up How do you find an experimental probability of a simple event?

#### Class.



**12.2** Independent Practice

COMMON CORE 7.SP.6, 7.SP.7b

**4.** Dree rolls a strike in 6 out of the 10 frames of bowling. What is the experimental probability that Dree will roll a strike in the first frame of the next game? Explain why a number cube would not be a good way to simulate this situation.

- 5. To play a game, you spin a spinner like the one shown. You win if the arrow lands in one of the areas marked "WIN". Lee played this game many times and recorded her results. She won 8 times and lost 40 times. Use Lee's data to explain how to find the experimental probability of winning this game.
- 6. The names of the students in Mr. Hayes' math class are written on the board. Mr. Hayes writes each name on an index card and shuffles the cards. Each day he randomly draws a card, and the chosen student explains a math problem at the board. What is the probability that Ryan is chosen today? What is the probability that Ryan is **not** chosen today?

Anna	Alisha	Kenna	Bridget
Meghan	Cody	Parker	Grace
Michael	Gabe	Taylor	Joel
Kate	Kaylee	Shaw	Tessa
Jon	Ryan	Morgan	Leo
_			

**7. Critique Reasoning** A meteorologist reports an 80% chance of precipitation. Is this an example of experimental probability, written as a percent? Explain your reasoning.



- **8.** Mica and Joan are on the same softball team. Mica got 8 hits out of 48 times at bat, while Joan got 12 hits out of 40 times at bat. Who do you think is more likely to get a hit her next time at bat? Explain.
- **9.** Make a Prediction In tennis, Gabby serves an ace, a ball that can't be returned, 4 out of the 10 times she serves. What is the experimental probability that Gabby will serve an ace in the first match of the next game? Make a prediction about how many aces Gabby will have for the next 40 serves. Justify your reasoning.
- **10. Represent Real-World Problems** Patricia finds that the experimental probability that her dog will want to go outside between 4 P.M. and 5 P.M. is  $\frac{7}{12}$ . About what percent of the time does her dog **not** want to go out between 4 P.M. and 5 P.M.?



FOCUS ON HIGHER ORDER THINKING

- **11.** Explain the Error Talia tossed a penny many times. She got 40 heads and 60 tails. She said the experimental probability of getting heads was  $\frac{40}{60}$ . Explain and correct her error.
- **12.** Communicate Mathematical Ideas A high school has 438 students, with about the same number of males as females. Describe a simulation to predict how many of the first 50 students who leave school at the end of the day are female.

**13. Critical Thinking** For a scavenger hunt, Chessa put one coin in each of 10 small boxes. Four coins are quarters, 4 are dimes, and 2 are nickels. How could you simulate choosing one box at random? Would you use the same simulation if you planned to put these coins in your pocket and choose one? Explain your reasoning.

Work Area

# **12.3** Experimental Probability of Compound Events

COMMON CORE 7.SP.8

Find probabilities of compound events using... tables, ..., and simulation. *Also* 7.SP.8a, 7.SP.8b, 7.SP.8c

ESSENTIAL QUESTION

How do you find the experimental probability of a compound event?

#### EXPLORE ACTIVITY

COMMON 7.SP.8a, 7.SP.8b

# **Exploring Compound Probability**

A **compound event** is an event that includes two or more simple events, such as flipping a coin *and* rolling a number cube. A compound event can include events that depend on each other or are independent. Events are independent if the occurrence of one event does not affect the probability of the other event, such as flipping a coin and rolling a number cube.

A What are the possible outcomes of flipping a coin once?

**B** What are the possible outcomes of rolling a standard number cube once?

C Complete the list for all possible outcomes for flipping a coin *and* rolling a number cube.

H1, H2, \_\_\_\_\_, \_\_\_\_, \_\_\_\_, T1, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_,

There are \_\_\_\_\_\_ possible outcomes for this compound event.

P Flip a coin and roll a number cube 50 times. Use tally marks to record your results in the table.

	1	2	3	4	5	6
н						
т						

**E** Based on your data, which compound event had the greatest experimental probability and what was it? The least experimental

probability? \_\_\_\_\_

**F** Draw Conclusions Did you expect to have the same probability for each possible combination of flips and rolls? Why or why not?

H1 would mean the coin landed on heads, and the number cube showed a 1.



# **Calculating Experimental Probability** of Compound Events

The experimental probability of a compound event can be found using recorded data.

EXAMPLE 1 Real

COMMON 7.SP.8, 7.SP.8a

A food trailer serves chicken and records the order size and sides on their orders, as shown in the table. What is the experimental probability that the next order is for 3-pieces with cole slaw?

	Green Salad	Macaroni & Cheese	French Fries	Cole Slaw
2 pieces	33	22	52	35
3 pieces	13	55	65	55

**STEP 1** 

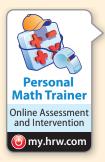
Find the total number of trials, or orders.

- 33 + 22 + 52 + 35 + 13 + 55 + 65 + 55 = 330
- **STEP 2** Find the number of orders that are for 3 pieces with cole slaw: 55.

**STEP 3** Find the experimental probability.

 $P(3 \text{ piece} + \text{slaw}) = \frac{\text{number of 3 piece} + \text{slaw}}{\text{total number of orders}}$  $= \frac{55}{330} \qquad \text{Substitute the values.}$  $= \frac{1}{6} \qquad \text{Simplify.}$ 

The experimental probability that the next order is for 3 pieces of chicken with cole slaw is  $\frac{1}{6}$ .



Math Talk

**Mathematical Practices** 

Javier said the total number of orders is 8 and not 330.

Is he correct? Explain.

YOUR TURN

 Drink sales for an afternoon at the school carnival were recorded in the table. What is the experimental probability that the next drink is a small cocoa?

	Soda	Water	Сосоа
Small	77	98	60
Large	68	45	52

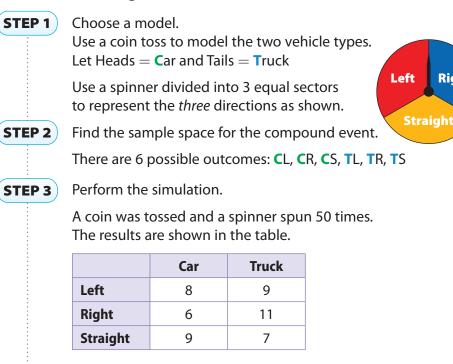
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# Using a Simulation to Make a Prediction

You can use a simulation or model of an experiment to find the experimental probability of compound events.

#### EXAMPLE 2 🎇

At a street intersection, a vehicle is classified either as a *car* or a *truck*, and it can turn *left*, *right*, or go *straight*. About an equal number of cars and trucks go through the intersection and turn in each direction. Use a simulation to find the experimental probability that the next vehicle will be a car that turns right.



STEP 4

Find the experimental probability that a car turns right.

$$P(\text{Car turns right}) = \frac{\text{frequency of compound event}}{\text{total number of trials}}$$
$$= \frac{6}{50} \qquad \text{Substitute the values.}$$
$$= \frac{3}{25} \qquad \text{Simplify.}$$

Based on the simulation, the experimental probability is  $\frac{3}{25}$  that the next vehicle will be a car that turns right.

#### Reflect

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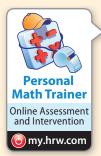
**2.** Make a Prediction Predict the number of cars that turn right out of 100 vehicles that enter the intersection. Explain your reasoning.

# Math On the Spot

7.SP.8c

Right

# My Notes





**3.** A jeweler sells necklaces made in three sizes and two different metals. Use the data from a simulation to find the experimental probability that the next necklace sold is a 20-inch gold necklace.

	Silver	Gold
12 in.	12	22
16 in.	16	8
20 in.	5	12

#### **Guided Practice**

 A dentist has 400 male and female patients that range in ages from 10 years old to 50 years old and up as shown in the table. What is the experimental probability that the next patient will be female and in the age range 22–39? (Explore Activity and Example 1)

	Range: 10–21	Range: 22–39	Range: 40–50	Range: 50+
Male	44	66	32	53
Female	36	50	45	74

2. At a car wash, customers can choose the type of wash and whether to use the interior vacuum. Customers are equally likely to choose each type of wash and whether to use the vacuum. Use a simulation to find the experimental probability that the next customer purchases a deluxe wash and no interior vacuum. Describe your simulation. (Example 2)



#### **ESSENTIAL QUESTION CHECK-IN**

3. How do you find the experimental probability of a compound event?

#### Class



**4. Represent Real-World Problems** For the same food trailer mentioned in Example 1, explain how to find the experimental probability that the next order is two pieces of chicken with a green salad.

The school store sells spiral notebooks in four colors and three different sizes. The table shows the sales by size and color for 400 notebooks.

	Red	Green	Blue	Yellow
100 Pages	55	37	26	12
150 Pages	60	44	57	27
200 Pages	23	19	21	19

- 5. What is the experimental probability that the next customer buys a red notebook with 150 pages?
- **6.** What is the experimental probability that the next customer buys any red notebooks?
- **7. Analyze Relationships** How many possible combined page count and color choices are possible? How does this number relate to the number of page size choices and to the number of color choices?
- A middle school English teacher polled random students about how many pages of a book they read per week.
  - Critique Reasoning Jennie says the experimental probability that a 7th grade student reads at least 100 pages per week is <sup>16</sup>/<sub>125</sub>. What is her error and the correct experimental probability?

	6th	7th	8th
75 Pages	24	18	22
100 Pages	22	32	24
150 Pages	30	53	25

**9.** Analyze Relationships Based on the data, which group(s) of students should be encouraged to read more? Explain your reasoning.

#### FOCUS ON HIGHER ORDER THINKING

- **10.** Make a Conjecture Would you expect the probability for the simple event "rolling a 6" to be greater than or less than the probability of the compound event "rolling a 6 and getting heads on a coin"? Explain.
- **11.** Critique Reasoning Donald says he uses a standard number cube for simulations that involve 2, 3, or 6 equal outcomes. Explain how Donald can do this.

 Draw Conclusions Data collected in a mall recorded the shoe styles worn by 150 male and for 150 female customers. What is the probability that the next customer is male and has an open-toe

HOT

	Male	Female
Open toe	11	92
Closed toe	139	58

shoe (such as a sandal)? What is the probability that the next male customer has an open-toe shoe? Are the two probabilities the same? Explain.

- **13.** What If? Suppose you wanted to perform a simulation to model the shoe style data shown in the table. Could you use two coins? Explain.
- **14. Represent Real-World Problems** A middle school is made up of grades 6, 7, and 8, and has about the same number of male and female students in each grade. Explain how to use a simulation to find the experimental probability that the first 50 students who arrive at school are male and 7th graders.

# **12.4** Making Predictions with Experimental Probability



Approximate the probability of a chance event by collecting data on the chance process that produces it..., and predict the approximate relative frequency given the probability. *Also* 7.RP.2c, 7.RP.3, 7.NS.3

Math On the Spo

my.hrw.com

**ESSENTIAL QUESTION** 

How do you make predictions using experimental probability?

EXPLORE ACTIVITY



# Using Experimental Probability to Make a Prediction

Real

Scientists study data to make predictions. You can use probabilities to make predictions in your daily life.

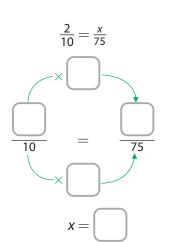
**EXAMPLE 1** Danae found that the experimental probability of her making a bull's-eye when throwing darts is  $\frac{2}{10}$ , or 20%. Out of 75 throws, about how many bull's-eyes could she predict she would make?

#### Method 1: Use a proportion.

Write a proportion. 2 out of 10 is how many out of 75?

Since 10 times \_\_\_\_\_ is 75, multiply

2 times \_\_\_\_\_ to find the value of *x*.



 $\times$  75 = x

15 = x



You can write probabilities as

ratios, decimals, or percents.

#### Method 2: Use a percent equation.

Write an equation to find 20% of 75.

Multiply.

Danae can predict that she will make about 15 bull's-eye throws out of 75.



**1.** A car rental company sells accident insurance to 24% of its customers. Out of 550 customers, about how many customers are predicted to



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purchase insurance? \_



# Using Experimental Probability to Make a Qualitative Prediction

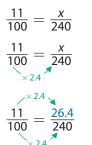
A prediction is something you reasonably expect to happen in the future. A qualitative prediction helps you decide which situation is more likely in general.

#### EXAMPLE 2 Real

COMMON CORE 7.SP.6

A doctor's office records data and concludes that, on average, 11% of patients call to reschedule their appointments per week. The office manager predicts that 23 appointments will be rescheduled out of the 240 total appointments during next week. Explain whether the prediction is reasonable.

#### Method 1: Use a proportion.



x = 26.4

26.4 is the average number of patients that would call to reschedule.

Write a proportion. 11 out of 100 is how many out of 240?
Since 100 times 2.4 is 240, multiply 11 times 2.4 to find the value of x.

#### Method 2: Use a percent equation.

$0.11 \cdot 240 = x$	Find 11% of 240.
26.4 = <i>x</i>	Solve for x.

The prediction of 23 is reasonable but a little low, because 23 is a little less than 26.4.

#### Reflect

2. Does 26.4 make sense for the number of patients?

YOUR TURN

**3.** In emails to monthly readers of a newsletter 3% of the emails come back undelivered. The editor predicts that if he sends out 12,372 emails, he will receive 437 notices for undelivered email. Do you agree with his prediction?

Explain.

# **Making a Quantitative Prediction**

You can use proportional reasoning to make quantitative predictions and compare options in real-world situations.

#### EXAMPLE 3 Prob

An online poll for a movie site shows its polling results for a new movie. If a newspaper surveys 150 people leaving the movie, how many people can it predict will like the movie based on the online poll? Is the movie site's claim accurate if the newspaper has 104 people say they like the movie?

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	Did you like the movie? Yes									
									7	2%
N	0				28%	)				ļ

7.SP.6

#### Analyze Information

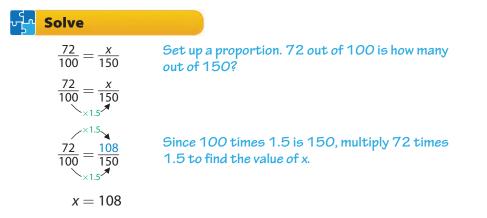
The **answer** is a prediction for how many people out of 150 will like the movie based on the online poll. Also tell whether the 104 people that say they like the movie is enough to support the movie site's claim.

#### List the important information:

- The online poll says 72% of movie goers like the new movie.
- A newspaper surveys 150 people.

#### Formulate a Plan

Use a proportion to calculate 72% of the 150 people surveyed.



The newspaper can predict that 108 out of 150 people will say they like the movie, based on the online poll.

#### Justify and Evaluate

Since 108 is close to 104, the newspaper survey and the online poll show that about the same percent of people like the movie.





4. On average, 24% of customers who buy shoes in a particular store buy two or more pairs. One weekend, 350 customers purchased shoes. How many can be predicted to buy two or more pairs? If 107 customers buy more than two pairs, did more customers than normal buy two or more pairs?

#### **Guided Practice**

- **1.** A baseball player reaches first base 30% of the times he is at bat. Out of 50 times at bat, about how many times will the player reach first base? (Explore Activity Example 1)
- **2.** The experimental probability that it will rain on any given day in Houston, Texas, is about 15%. Out of 365 days, about how many days can residents predict rain? (Explore Activity Example 1)
- **3.** A catalog store has 6% of its orders returned for a refund. The owner predicts that a new candle will have 812 returns out of the 16,824 sold. Do you agree with this prediction? Explain. (Example 2)
- 4. On a toy assembly line, 3% of the toys are found to be defective. The quality control officer predicts that 872 toys will be found defective out of 24,850 toys made. Do you agree with this prediction? Explain. (Example 2)
- 5. A light-rail service claims to be on time 98% of 6. On average, a college claims to accept the time. Jeanette takes the light-rail 40 times one month, how many times can she predict she will be on time? Is the light-rail's claim accurate if she is late 6 times? (Example 3)
- 18% of its applicants. If the college has 5,000 applicants, predict how many will be accepted. If 885 applicants are accepted, is the college's claim accurate? (Example 3)

#### **ESSENTIAL QUESTION CHECK-IN**

7. How do you make predictions using experimental probability?

# **12.4 Independent Practice**

COMMON 7.SP.6

The table shows the number of students in a middle school at the beginning of the year and the percentage that can be expected to move out of the area by the end of the year.

- 8. How many 7th grade students are expected to move by the end of the year? If 12 students actually moved, did more or fewer 7th grade students move than expected? Justify your answer.
- 6th
   7th
   8th

   Number of Students
   250
   200
   150

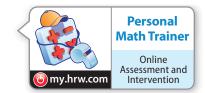
   % Moves
   2%
   4%
   8%

**9. Critique Reasoning** The middle school will lose some of its funding if 50 or more students move away in any year. The principal claims he only loses about 30 students a year. Do the values in the table support his claim? Explain.

Class.

**10. Represent Real-World Problems** An airline knows that, on average, the probability that a passenger will not show up for a flight is 6%. If an airplane is fully booked and holds 300 passengers, how many seats are expected to be empty? If the airline overbooked the flight by 10 passengers, about how many passengers are expected to show up for the flight? Justify your answer.

**11. Draw Conclusions** In a doctor's office, an average of 94% of the clients pay on the day of the appointment. If the office has 600 clients per month, how many are expected not to pay on the day of the appointment? If 40 clients do not pay on the day of their appointment in a month, did more or fewer than the average not pay?



**12.** Counterexamples The soccer coach claimed that, on average, only 80% of the team come to practice each day. The table shows the number of students that came to practice for 8 days. If the team has 20 members, how many team members should come to practice to uphold the coach's claim? Was the coach's claim accurate? Explain your reasoning.

	1	2	3	4	5	6	7	8
Number of Students	18	15	18	17	17	19	20	20

**13.** What's the Error? Ronnie misses the school bus 1 out of every 30 school days. He sets up the proportion  $\frac{1}{30} = \frac{180}{x}$  to predict how many days he will miss the bus in the 180-day school year. What is Ronnie's error?

#### FOCUS ON HIGHER ORDER THINKING

**14.** Persevere in Problem Solving A gas pump machine rejects 12% of credit card transactions. If this is twice the normal rejection rate for a normal gas pump, how many out of 500 credit cards transactions would a

normal gas pump machine reject? \_

**15.** Make Predictions An airline's weekly flight data showed a 98% probability of being on time. If this airline has 15,000 flights in a year, how many flights would you predict to arrive on time? Explain whether you can use the data to predict whether a specific flight with this airline will be on time.

**16. Draw Conclusions** An average response rate for a marketing letter is 4%, meaning that 4% of the people who receive the letter respond to it. A company writes a new type of marketing letter, sends out 2,400 of them, and gets 65 responses. Explain whether the new type of letter would be considered to be a success.

#### Work Area

HOT

#### **MODULE QUIZ**



#### 12.1 Probability

1. Josue tosses a coin and spins the spinner at the right. What are all the possible outcomes?

#### **12.2 Experimental Probability of Simple Events**

**2.** While bowling with friends, Brandy rolls a strike in 6 out of 10 frames. What is the experimental probability that Brandy will roll

a strike in the first frame of the next game?

**3.** Ben is greeting customers at a music store. Of the first 20 people he sees enter the store, 13 are wearing jackets and 7 are not. What is the experimental probability that the next person to enter the store will be wearing a jacket?

#### **12.3 Experimental Probability of Compound Events**

**4.** Auden rolled two number cubes and recorded the results.

Roll #1	Roll #2	Roll #3	Roll #4	Roll #5	Roll #6	Roll #7
2, 1	4, 5	3, 2	2, 2	1, 3	6, 2	5, 3

What is the experimental probability that the sum of the next two numbers rolled is greater than 5?

#### 12.4 Making Predictions with Experimental Probability

**5.** A player on a school baseball team reaches first base  $\frac{3}{10}$  of the time he is at bat. Out of 80 times at bat, about how many times would you predict he will reach first base?



#### ESSENTIAL QUESTION

6. How is experimental probability used to make predictions?



MODULE 12 MIXED REVIEW Assessment Readiness



#### **Selected Response**

- A frozen yogurt shop offers scoops in cake cones, waffle cones, or cups. You can get vanilla, chocolate, strawberry, pistachio, or coffee flavored frozen yogurt. If you order a single scoop, how many outcomes are in the sample space?
  - (A) 3
    (C) 8
    (B) 5
    (D) 15
- 2. A bag contains 7 purple beads, 4 blue beads, and 4 pink beads. What is the probability of **not** drawing a pink bead?

(A) $\frac{4}{15}$	$\bigcirc \frac{8}{15}$
<b>B</b> $\frac{7}{15}$	(D) $\frac{11}{15}$

- **3.** During the month of June, Ava kept track of the number of days she saw birds in her garden. She saw birds on 18 days of the month. What is the experimental probability that she will see birds in her garden on July 1?
  - (A)  $\frac{1}{18}$  (C)  $\frac{1}{2}$ (B)  $\frac{2}{5}$  (D)  $\frac{3}{5}$
- **4.** A rectangle has a width of 4 inches and a length of 6 inches. A similar rectangle has a width of 12 inches. What is the length of the similar rectangle?
  - (A) 8 inches (C) 14 inches
  - (B) 12 inches (D) 18 inches
- The experimental probability of hearing thunder on any given day in Ohio is 30%. Out of 600 days, on about how many days can Ohioans expect to hear thunder?
  - (A) 90 days (C) 210 days
  - (B) 180 days (D) 420 days

**6.** Isidro tossed two coins several times and then recorded the results in the table below.

Toss 1	Toss 2	Toss 3	Toss 4	Toss 5	
H; T	Т; Т	T; H	H; T	H; H	

What is the experimental probability that both coins will land on the same side on Isidro's next toss?

(A) $\frac{1}{5}$	$\bigcirc \frac{3}{5}$
<b>B</b> $\frac{2}{5}$	<b>D</b> $\frac{4}{5}$

#### Mini-Task

 Magdalena had a spinner that was evenly divided into sections of red, blue, and green. She spun the spinner and tossed a coin several times. The table below shows the results.

Trial 1	Trial 2	Trial 3	Trial 4	Trial 5	
blue; T	green; T	green; H	red; T	blue; H	

- a. What are all the possible outcomes?
- **b.** What experimental probability did Magdalena find for spinning blue? Give your answer as a fraction in simplest form, as a decimal, and as a percent.
- c. Out of 90 trials, how many times should Magdalena predict she will spin green while tossing tails?